

Evaluating More Complex Boolean Expressions. One tool that can be used to evaluate a Boolean expression is a Truth Table.

Truth Table for the AND, OR, and NOT logical operators.

P	Q	P && Q	P Q	!P
True	True			
True	False			
False	True			
False	False			

Operator Precedence

_____ (highest)

 _____ (lowest)

Evaluate the following.

!(!B) is equivalent to _____

!a && b == c || d where c is TRUE and a, b, d are FALSE _____

Some Useful Boolean Equivalences

Let a and b represent algebraic value

!(a < b) is equivalent to _____
 !(a == b) is equivalent to _____
 !(a >= b) is equivalent to _____

c is true, a,b,d false answer the following carefully:

a || b != c || d == b _____ a || d && c _____
 !(a == b) && b || c == d _____ !(a || d) && c _____
 a || b || d && c _____ (a && d) || true _____
 !(a || b || d) && c _____ false || !d _____
 !(a || b || d) && !c _____ true && !d _____

Let p and q and r represent boolean values

!(p && q) is equivalent to _____
 !(p || q) is equivalent to _____

DeMorgan's
Laws

Some sample problems.

- 1) Simplify !(3 <= x && x <= 5)
- 2) For what values of p and q is this expression TRUE?
(p && q) || !(p || q)
- 3) What value(s) will this print?
System.out.println(!(x > 10 || x < 20));
- 4) Simplify !(x != 0 || y != 0)
- 5) Simplify !(x < 5) || !(x >= 9)
- 6) When is this expression TRUE?
x > 7 && x < 5 || x > 10

Short-Circuit Evaluation

The JVM sometimes knows the value of a Boolean expression before it has evaluated all of its parts. For instance, in the expression

(p && q)

if p is _____, then the whole expression must be _____ (and the JVM will not bother to evaluate q).

In the same way, in this expression:

(p || q)

if p is _____, then the whole expression must be _____ (and the JVM will not bother to evaluate q).

1) If x has a value of zero, what happens?	int x; // x is assigned a value
2) If x has a value of 5, what happens?	if (x > 4 10.0 / (x - 5) > 0) System.out.println("A");
3) If x has a value of 3, what happens?	else if (10 / x < 0 x > 10) System.out.println("B"); else if (x > 5 && 1.0 / (x - 3) > 0) System.out.println("C"); else System.out.println("D");

Higher precedence: && or || you must know this!

Writing equivalent statements. Show the truth table to prove.

1. $\neg(p \ \&\& \ q) \ \&\& \ (p \ || \ q)$

2. $\neg((p \ || \ q) \ \&\& \ (q \ || \ !r))$

3. Given this statement: $(a < c) \ || \ \neg((c == a*b) \ \&\& \ (c < a))$

what are possible values of a, b, c that will make this true? (ie.. $a > c$ is false, etc)

will a truth table help? or assign values to parts of the statement?

4. Rewrite this statement more explicitly to show order:

$\neg A \ \&\& \ B \ || \ C$

6) Complete the Truth Table

P	Q	R	Q && R	P (Q && R)
True	True	False		
False	False	True		

7) Complete the Truth Table

P	Q	R	P && Q	P && R	(P && Q) (P && R)
True	False	True			
False	False	True			

8) List all the values of p, q, and r (where p, q, and r are boolean variables) that make this expression TRUE. *Can use a truth table.*

$$!p \&\& (q \parallel r)$$

9) List all the values of x that make this expression TRUE. Assume x is an int.

$$!(x > 5 \&\& x \leq 15)$$

10) Simplify (where p and q are boolean variables)

$$!(!p \&\& q)$$

11) Simplify (where p and q are boolean variables)

$$!(p \parallel !q)$$

12) If a boolean expression involved four different independent boolean variables/expressions (e.g. p, q, r, and s), how many different rows (i.e. combinations of values) would the Truth Table contain?

13) The boolean expression $!A \&\& B \parallel C$ is equivalent to

- a) $!A \&\& (B \parallel C)$
- b) $((!A) \&\& B) \parallel C$
- c) $(!A) \&\& (B \parallel C)$
- d) $!(A \&\& B) \parallel C$
- e) $!(A \&\& B \parallel C)$

14) Assume that a and b are integers. The boolean expression

`!(a <= b) && (a * b > 0)`

will always evaluate to true given that

- a) `a = b`
- b) `a > b`
- c) `a < b`
- d) `a > b and b > 0`
- e) `a > b and b < 0`

15) Given that a, b, and c are integers, consider the boolean expression

`(a < b) || !(c == a * b) && (c < a)`

Which of the following will guarantee that the expression is true?

- a) `c < a` is false
- b) `c < a` is true
- c) `a < b` is false
- d) `c == a * b` is true
- e) `c == a * b` is true, and `c < a` is true

16) If c and d are boolean variables, which one of the answer choices is NOT equivalent to the following expression?

`(c && d) != (c || d)`

- a) `(c && !d) || (!c && d)`
- b) `(c || d) && (!c && !d)`
- c) `(c || d) && (!c || !d)`
- d) `(c || d) && !(c && d)`
- e) `c != d`

17) Select the TRUE statement.

- a) there will be a compiler error due to `50/x`
- b) there will be a run-time error due to `50/x`
- c) the code will run and "ok" will be displayed.
- d) the code will run and "ok" will NOT be displayed.

```
int x = 0;
boolean alive = true;
if (alive || 50 / x != 0)
    System.out.println("ok");
```

18) m1 and m2 must each return a boolean.

True False

```
if ( m1() && m2() )
```

19) If m1 returns true, then method m2 will not be called.

True False

```
// code A
```

20) If m1 returns false, then method m2 will not be called.

True False

```
else
```

```
// code B
```

Precedence Chart with Logical Operators – Unit 3

Grouping	()	N/A
Method selector	.	left to right
unary plus/minus/not	+ - !	N/A
multiplicative	* / %	left to right
additive	+ -	left to right
relational operators	< <= > >= == !=	N/A
And	&&	left to right
Or		left to right
Assignment Operators left	= += *= -= /= %=	right to